

Oct. 7

Word problems

1) Figure out inputs and outputs

2) Understand relationship between inputs + output

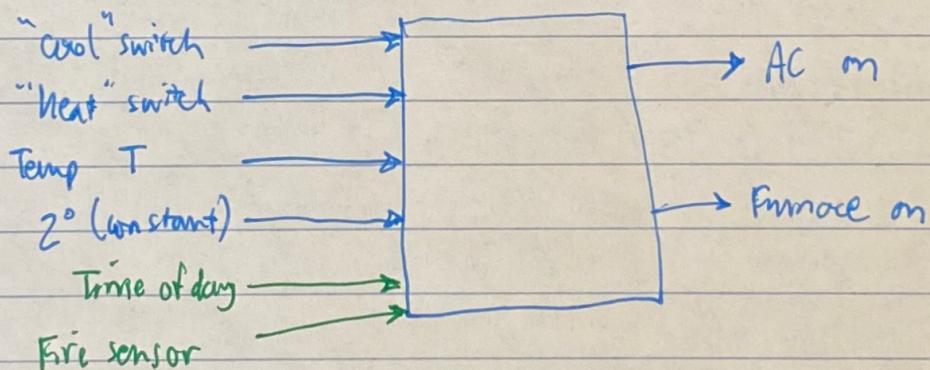
3) Write an expression for each output

- Each output is an independent problem

Ex: Thermostat for HVAC

1) AC on if "cool" on and Temp $\geq 2^\circ + \text{setting}$

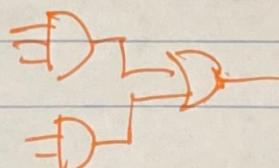
2) Furnace on if "heat" on " " $\leq \text{setting} - 2^\circ$



Methods to describe Boolean expressions:

1) Simple English (if $A=1$ and $B=0$, then $\text{out}=1$)

2) Circuit schematic



2

3) Truth Table

enumerate all input combinations

input(s)	output(s)
1	1
1	1
1	1

4) Expression

$$A + B \cdot C, \text{ SOP, POS}$$

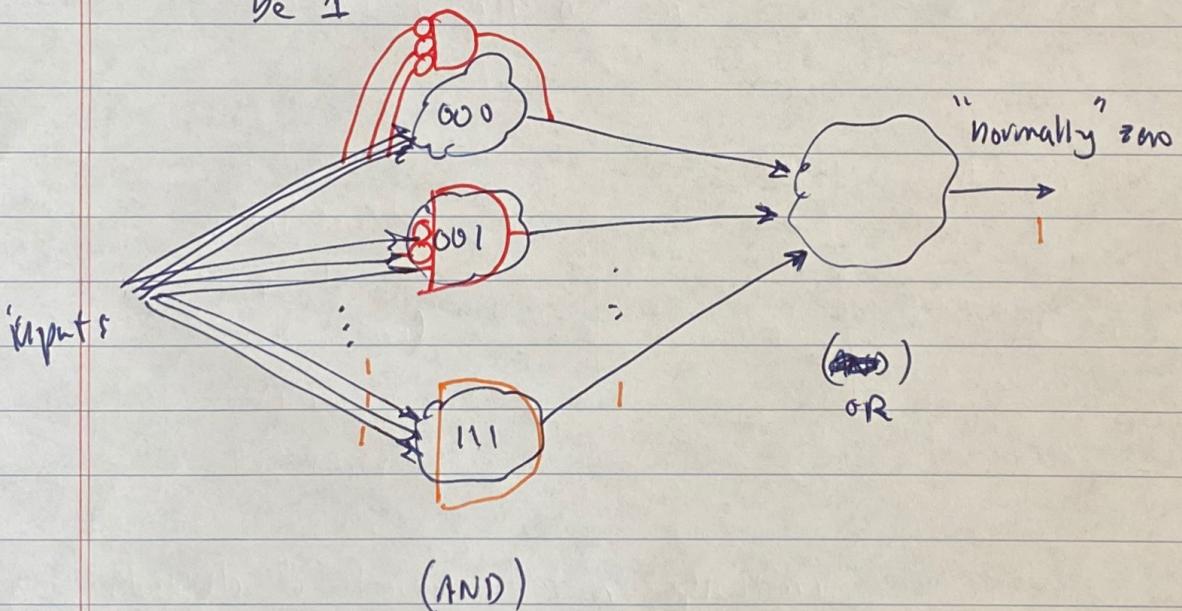
5) Min term

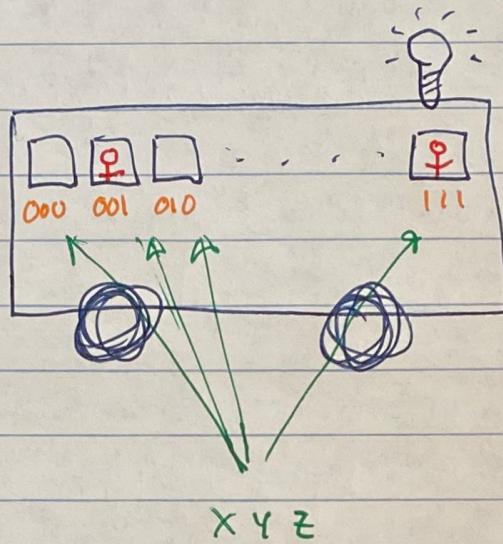
6) Maxterm

Min terms

SOP expression

Enumerate combinations of inputs which give the output to be 1





Truth table

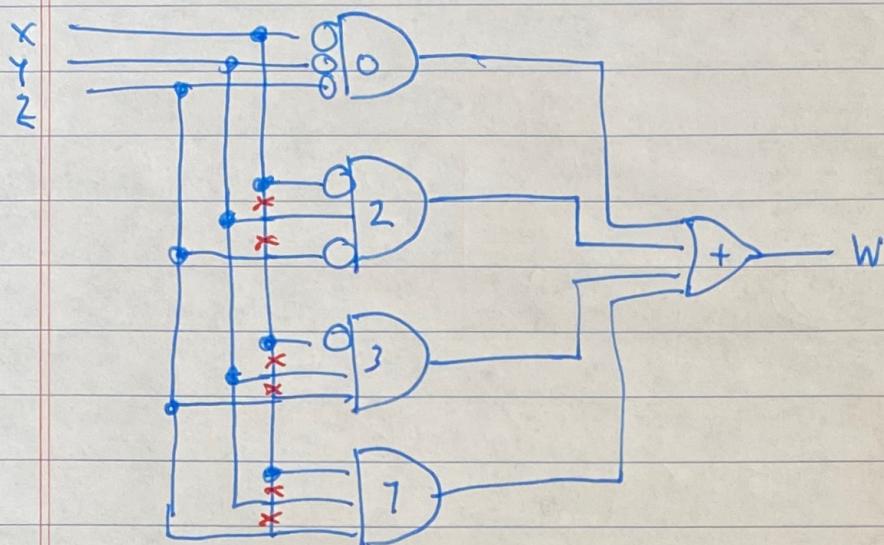
X Y Z	X Y Z	W
0 0 0	000 = binary "0" = 0 ₁₀	1 ←
0 0 1	"1" = 1 ₁₀	0
0 1 0	2	1 ←
0 1 1		1 ←
1 0 0		0
1 0 1		0
1 1 0		0
1 1 1	2 ₁₀	1 ←

$$W = m_0 + m_2 + m_3 + m_7$$

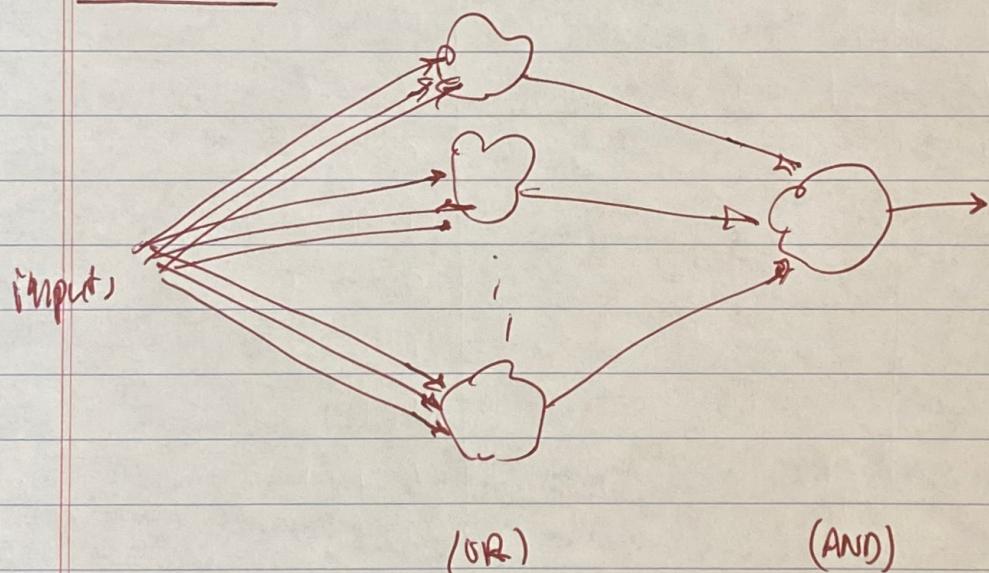
$$W = X' \cdot Y' \cdot Z' + X' \cdot Y \cdot Z' + X \cdot Y \cdot Z + X \cdot Y \cdot Z$$

SOP

$$W = \sum m(0, 2, 3, 7)$$



Maxterms



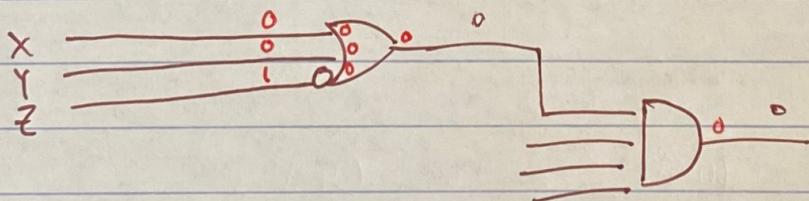
P.O.S. expression where each entry in a T.T. is a potential Maxterm

X	Y	Z		W
0	0	0	$X + Y + Z = M_0$	1
0	0	1	$X + Y + Z' = M_1$	0 ←
0	1	0	$X + Y' + Z = M_2$	1
0	1	1		1
1	0	0		0 ←
1	0	1		0 ←
1	1	0		0 ←
1	1	1	$X' + Y' + Z' = M_7$	1

$$W = \underline{M_1} \cdot M_4 \cdot M_5 \cdot M_6$$

$$= \prod M(1, 4, 5, 6)$$

$$= \underbrace{(X + Y + Z')}_{M_1} \cdot (X' + Y + Z) \cdot (X' + Y + Z') \cdot (X' + Y' + Z)$$



- No common terms between min term & max term expansions of the same function
- All 2^n ($n = \text{# of inputs}$) terms in min term or max term expansion

X	Y	Z	Z'
00		1	0
01		1	0
10		1	0
11		0	1

$$Z = \sum m(0,1,2) = \Pi M(3)$$

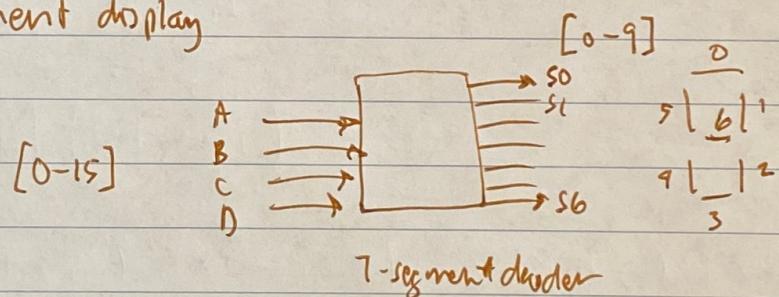
$$Z' = \sum m(3) = \Pi M(0,1,2)$$

Incompletely-Specified Functions

"Don't Care" = X

~ third value for variables

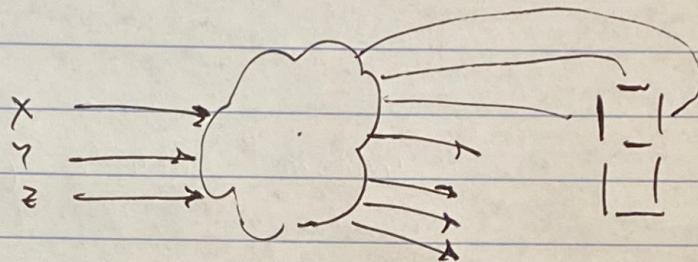
Ex: 7-segment display



A	B	C	D	s ₀	s ₁	s ₂	s ₃	s ₄	s ₅	s ₆
0000	0			1	1	1	1	1	1	0
0001				0	1	1	0	0	0	0
⋮				⋮	⋮	⋮	⋮	⋮	⋮	⋮
1010				x	x	x	x	x	x	x
⋮				?	1	?	1	?	?	1
1111				x	x	x	x	x	x	x

$$S_0 = \sum m(\cancel{0}, 2, 3, \dots) + \sum d(10, 11, 12, 13, 14, 15)$$

$$S_0 = \pi M(1, 4, \dots) - \pi D(10, 11, 12, 13, 14, 15)$$



x	y	z	-	-	-	-	-	-
0	0	0	1	0	0	0		
-	-	-						
-	-	-						
-	-	-						
-	-	-						