

1 CMOS Inverter Amplifier

Figure 1 shows a CMOS inverter biased as a linear amplifier. For this problem, use the transistor parameters in Table 1.

Parameter	NMOS	PMOS
V_t	1 V	-1 V
L_d	0	0
X_d	0	0
k'	$300 \mu\text{A}/\text{V}^2$	$100 \mu\text{A}/\text{V}^2$
γ	0	0
W/L	2	6
λ	0.1 V^{-1}	0.1 V^{-1}

Table 1: Problem 1 Transistor Parameters.

Problem 1.1 (3 points) Assume $V_I = 1.5 \text{ V}$. For what range of V_O will the circuit best act as an amplifier? What is the output voltage swing?

Want M1 + M2 in saturation:

$$V_{GS1} = V_I = 1.5 \text{ V}, V_{OV1} = 0.5 \text{ V} \Rightarrow V_{out} \geq 0.5 \text{ V}$$

$$V_{GS2} = V_{DD} - V_I = 1.5 \text{ V}, V_{OV2} = 0.5 \text{ V} \Rightarrow V_{out} \leq 2.5 \text{ V}$$

$$0.5 \text{ V} \leq V_{out} \leq 2.5 \text{ V}$$

$$\begin{aligned} \text{Output Swing} &= 2 \text{ V as amplifier} \\ &= 3 \text{ V } (0 \leq V_O \leq V_{DD}) \text{ for output levels} \end{aligned}$$

Problem 1.2 (2 points) Find the power dissipation assuming the bias conditions in Problem 1.1.

$$I_{D1} = I_{D2} = \frac{k'_n}{2} \left(\frac{W}{L}\right)_n (V_I - V_{tn})^2 = \frac{300 \mu\text{A}/\text{V}^2}{2} (2) (1.5 \text{ V} - 1)^2$$

$$= 75 \mu\text{A} \quad (86.2 \mu\text{A} \text{ if } \lambda = 0.1 \text{ V}^{-1})$$

$$P = I_{D1} V_{DD} = 225 \mu\text{W}$$