# EEC 118 Spring 2011 Homework #4

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Reading: Rabaey Chapters 6.2 and 7.1-7.3 [1].

**Reference:** Kang and Leblebici Chapters 7 and 8 [2].

### 1 Enhancement Load Logic Circuit

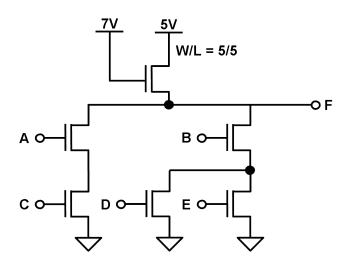


Figure 1: NMOS enhancement load complex gate.

For the enhancement load logic gate shown in Figure 1,

- Pull-up transistor W/L = 5/5
- Pull-down transistors W/L=100/5
- $V_{T0,n} = 1.0 \text{V}$
- $\bullet \ \lambda = 0.0 \mathrm{V}^{-1}$

- $\mu_n C_{ox} = 100 \mu A/V^2$
- $\gamma = 0.4 V^{1/2}$
- $|2\phi_F| = 0.6$ V

**Problem 1.1** Write a Boolean expression for the output F as a function of the inputs.

**Problem 1.2** Identify the worst-case input combination(s) for  $V_{OL}$ .

**Problem 1.3** Calculate the worst-case value of  $V_{OL}$ . Assume that all pull-down transistors have the same body bias and that, initially,  $V_{OL} \approx 5\%$  of  $V_{DD} = 5$ V.

**Problem 1.4** Does the value of  $V_{OL}$  depend on  $k_n = \mu_n C_{ox}$ ? Explain why or why not.

## 2 Two Input CMOS NOR Gate

**Problem 2.1** Calculate  $V_{OL}$ ,  $V_{OH}$ ,  $V_{IL}$ ,  $V_{IH}$ ,  $NM_L$ , and  $NM_H$  for a two input CMOS NOR gate. Assume for the transistors the following parameters:  $V_{T0,n} = 0.7$ V,  $V_{T0,p} = -0.7$ V,  $(W/L)_n = 1/1$ ,  $(W/L)_p = 4/1$ ,  $\mu_n C_{ox} = 40 \ \mu\text{A/V}^2$ ,  $\mu_p C_{ox} = 20 \ \mu\text{A/V}^2$ . Neglect  $\gamma$  and  $\lambda$ .  $V_{DD} = 5$ V. Assume that all inputs switch simultaneously.

## 3 Two Input CMOS NAND Gate

**Problem 3.1** Assume that a two input CMOS NAND gate drives a total load capacitance of 0.1pF. All devices have  $W=10\mu\mathrm{m}$ , but the effective length for NMOS devices  $L_{eff}=1\mu\mathrm{m}$  while for the PMOS devices  $L_{eff}=2\mu\mathrm{m}$ . Given that  $k_n'=20\mu\mathrm{A/V^2},\ k_p'=10\mu\mathrm{A/V^2},\ V_{T,n}=1.0\mathrm{V},\ V_{T,p}=-1.0\mathrm{V},\ \mathrm{and}\ V_{DD}=5\mathrm{V},\ \mathrm{approximate}\ t_{pLH}\ \mathrm{and}\ t_{pHL}.$ 

#### 4 Mixed Combinational and Sequential Logic

**Problem 4.1** A useful trick for highly optimized logic design is to fold a combinational CMOS circuit into a sequential circuit such as a latch. Modify the master stage latch circuit shown in Figure 7-26 in Rabaey to incorporate the logic function  $F = A \cdot (B + C)$ . Size the transistors such that the pullup and pulldown networks for the equivalent inverter have equal rise and fall times. Assume the mobility ratio  $\mu_n/\mu_p = 2.5$ ,  $V_{T0,n} = |V_{t0,p}|$ , and a minimum sized device has W/L = 5/1. Write your answer in terms of the W/L ratios for the PMOS and NMOS devices. Hint: See Figure 7-31.

### References

- [1] J. Rabaey, A. Chandrakasan, and B. Nikolic, *Digital Integrated Circuits: A Design Perspective*, 2nd ed. Upper Saddle River, New Jersey: Prentice-Hall, Inc., 2003.
- [2] S.-M. Kang and Y. Leblebici, *CMOS Digital Integrated Circuits: Analysis and Design*, 3rd ed. San Francisco: McGraw-Hill, Inc., 2003.