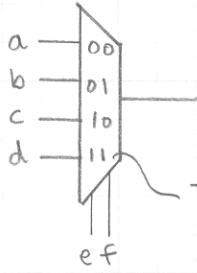


Mux Marking



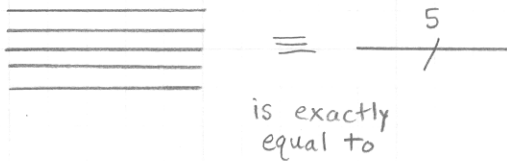
These values indicate which input is connected to the output when the control input(s) equal these values.

e	f	z
0	0	a
0	1	b
1	0	c
1	1	d

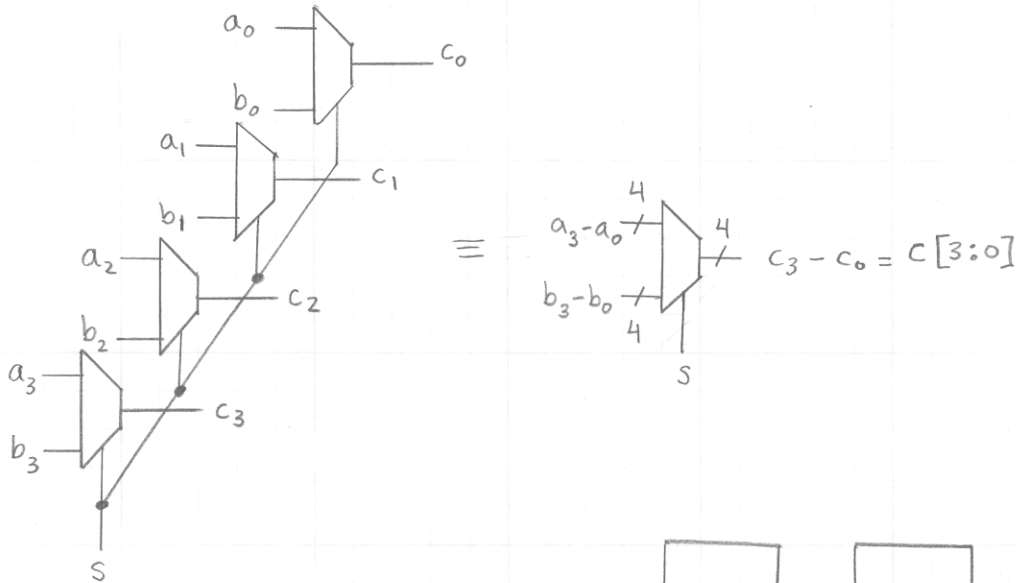
Bus Notation

A bus is a "bundle" of wires which are conceptually related (e.g., an 8-bit binary number on a set of 8 wires, each bit on its own wire)

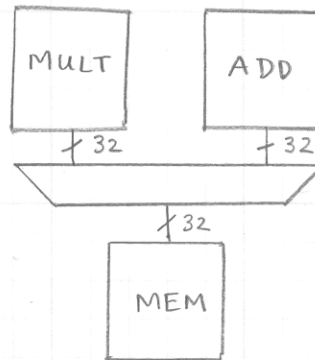
Shorthand bus notation:



Ex: We can stack up muxes in parallel to create multi-bit muxes

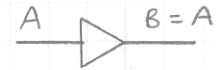


Ex: Routing results in a CPU

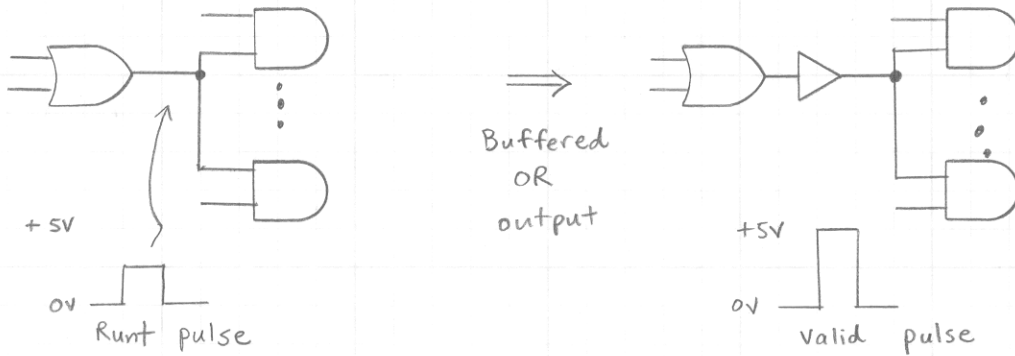


9.3 Three-State Buffers

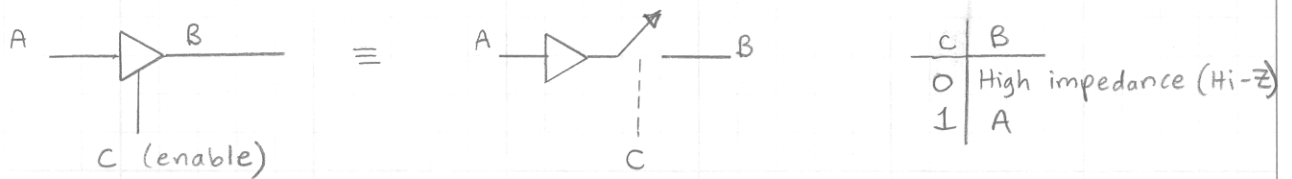
A buffer simply passes its inputs to its outputs:



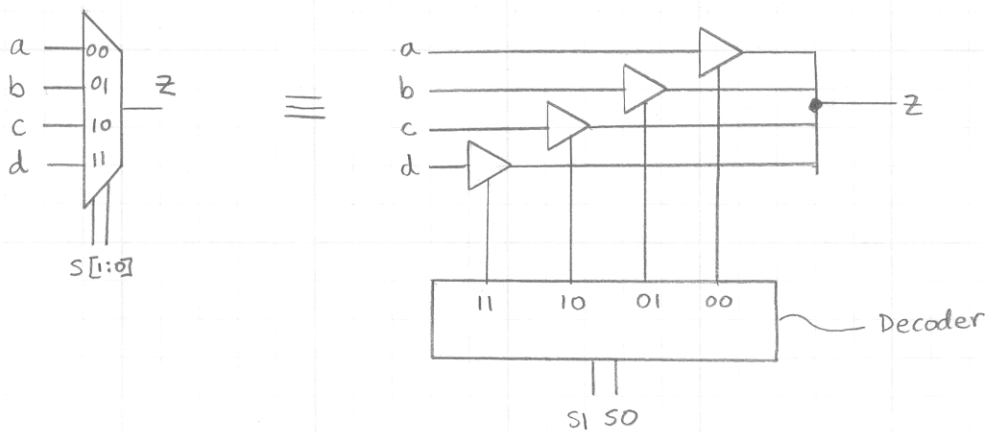
Logically, it does nothing, but electrically it can help drive a large number of loads:



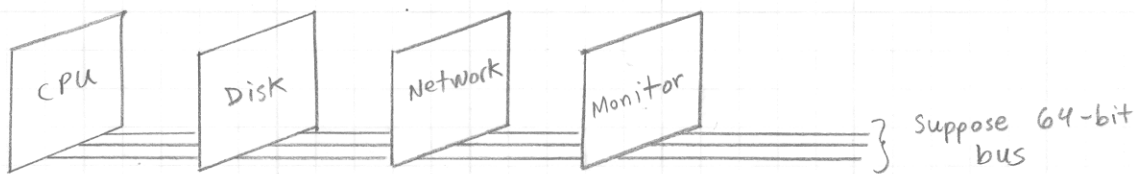
A three-state (tri-state) buffer has three output states: 0, 1, high impedance (disconnected)



Ex: Use tri-state buffers to build multiplexers:



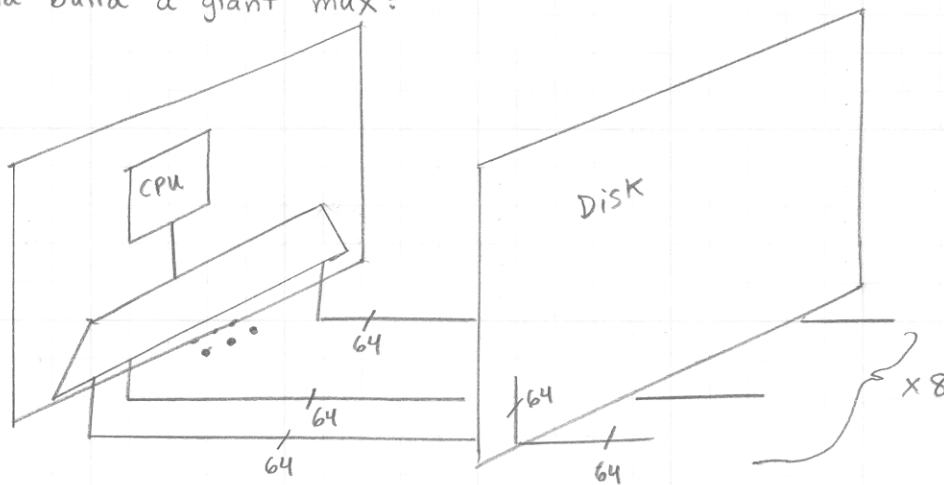
Ex: Suppose we need to communicate with one module at a time where there are from 1-8 modules. For example, on the PCI bus inside your computer:



13-782 500 SHEETS, FILLER 5 SQUARE
42-381 50 SHEETS, EYEGLASS 5 SQUARE
42-382 100 SHEETS, EYEGLASS 5 SQUARE
42-383 200 SHEETS, EYEGLASS 5 SQUARE
42-384 100 SHEETS, EYEGLASS 5 SQUARE
42-385 200 SHEETS, EYEGLASS 5 SQUARE
42-386 100 RECYCLED WHITE 5 SQUARE
42-387 200 RECYCLED WHITE 5 SQUARE
Made in U.S.A.

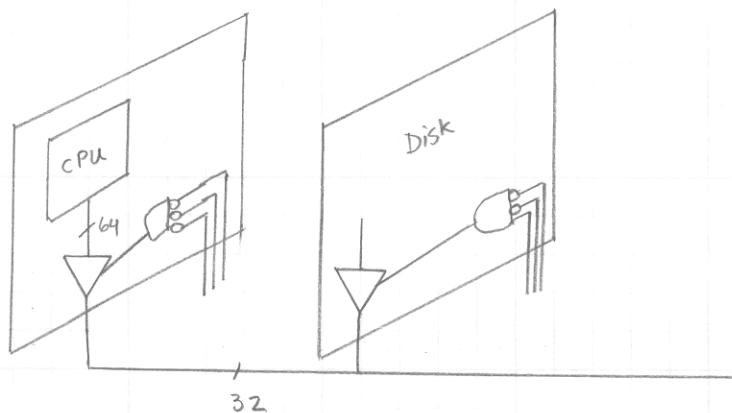


Could build a giant mux:



but the motherboard requires $64 \times 8 = 512$ signal wires!

Better to use tri-state buffers on each board and activate them when the three bit address matches:



Now we only have $64 + 3 = 67$ motherboard wires!

9.4 Decoders and Encoders

For some applications (like building a mux out of tri-state buffers), we need a box to "decode" selector bits into single enables:

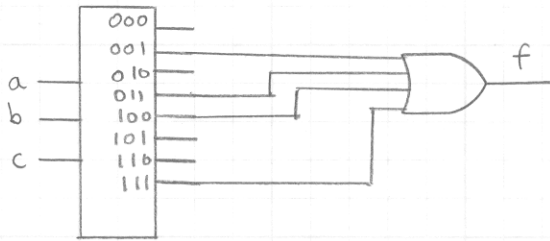
a	b	w	x	y	z
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

Only one output is high at a time.

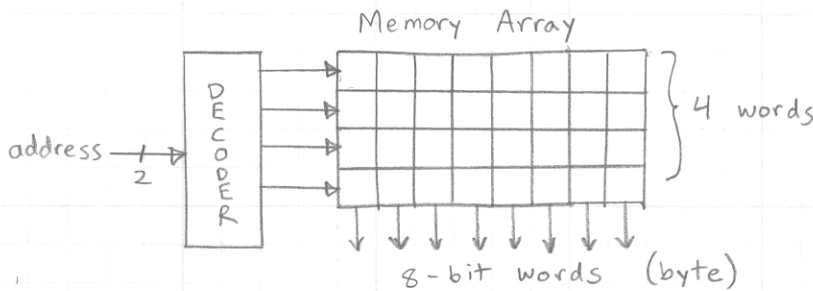
Called a decoder.

Each row generates exactly one minterm.

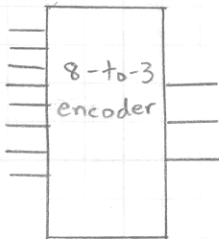
Ex: Use a decoder to generate a boolean function: $f(a,b,c) = \sum m(1,3,4,7)$



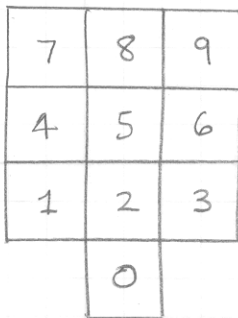
Ex: Also, an address decoder is an essential part of any multi-word memory:



An encoder performs the inverse operation of a decoder:



Ex: A touch-tone keypad:



⇒ 10 inputs, coded to 4-bit number

Also need an extra "valid" bit to indicate when the output is valid (i.e., a key is being pressed).

Encoder does this (valid is just OR of inputs), but what if more than 1 button is pushed simultaneously?

10 input bits ($k_0 - k_9$) ⇒ 1024 combinations
 4 output bits ⇒ 16 combinations

Possibility #1: Output is invalid if more than 1 key is pressed:

K_0	K_1	K_2	...	K_q	Output	Valid
0	0	0		0	XXXX	0
1	0	0		0	0000	1
0	1	0		0	0001	1
0	0	1		0	0010	1
	⋮			⋮	⋮	⋮
0	0	0	...	1	1001	1
1	1	0	...	0	XXXX	0
1	0	1	...	0	XXXX	0
1	0	0	...	1	XXXX	0
		⋮				

Need to specify many states!

Possibility #2: Highest number pressed wins

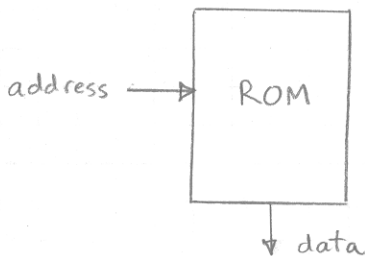
K_0	K_1	K_2	...	K_q	output	Valid
(single bit high cases same as above)					⋮	⋮
0	0	0	...	1	1001	1
X	1	0	...	0	0001	1
X	X	1	...	0	0010	1
X	X	X	...	1	1001	1
		⋮			⋮	⋮

Higher position inputs take priority over lower position inputs ⇒

called a priority encoder

9.5 Read-Only Memories (ROMs)

A Read-Only Memory (ROM) is a memory whose contents are permanent or semi-permanent (non-volatile)



• Can only read it (no writes during normal operation)

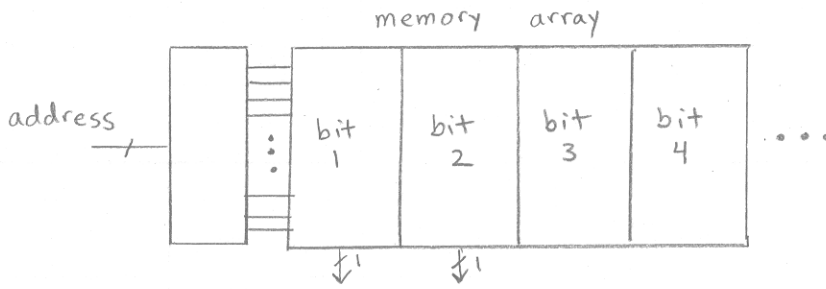
• For n address bits, there can be up to 2^n words in the memory

Specify contents with a truth table:

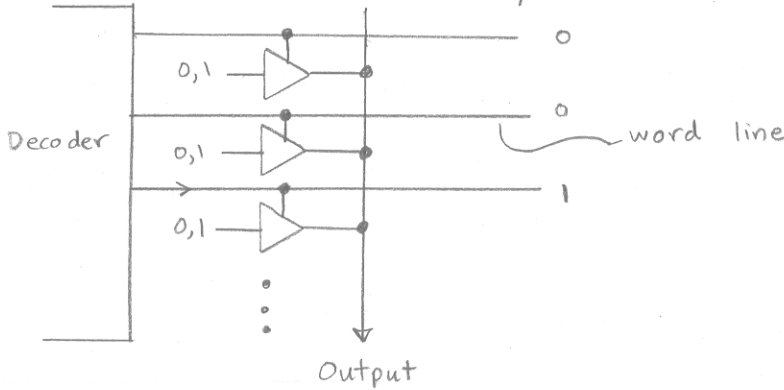
address	output
000	0
001	1
010	0
011	1
⋮	

} completely arbitrary values - we choose

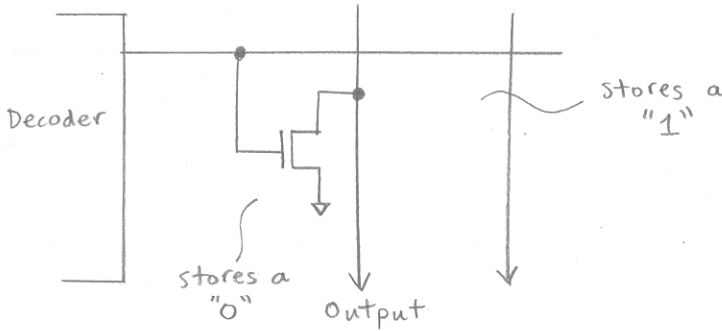




We can think of a ROM memory cell as a tri-state buffer: (enabled by decoder output)



We can also think of the ^{memory} cells as transistors:



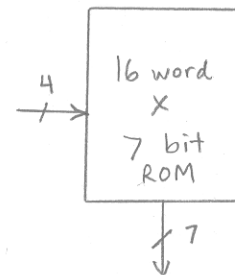
Think of the address decoder as a big mux which selects the activated memory row.

ROMs are the simplest implementation of a truth table - in fact, a truth table is how we specify a ROM!

A	B	C	D	E	F	G	H	I	J	K
0	0	0	0	0	1	0	1	0	1	1
0	0	0	1	1	1	0	0	0	0	1
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
1	1	1	1	0	0	1	0	1	1	0

4 address bits # output bits = 7

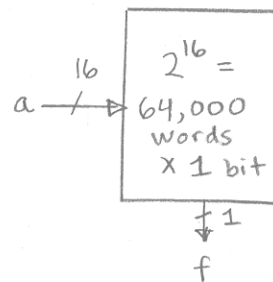
words in memory = 16



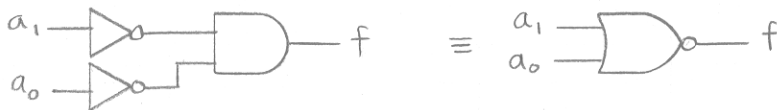
ROMs are a completely general solution for implementing combinational logic, but the solution depends on "randomness" of function, among other things.

Ex: Implement f is high when a 16-bit number $\{a_{15}, a_{14}, \dots, a_0\} = a[15:0]$ is a factor of 4

ROM:	a_{15}	a_{14}	\dots	a_3	a_2	a_1	a_0	f
	0	0		0	0	0	0	1
				0	0	0	1	0
		\vdots		0	0	1	0	0
				0	0	1	1	0
				0	1	0	0	1
				0	1	0	1	0



Logic: f is 1 when $a_1 = 0$ and $a_0 = 0$



Some types of ROMs:

1. Permanent (mask programmable): bits set when chip is made
2. One-time programmable (OTP) ROM, PROM
3. Electrically Erasable programmable ROM: EEPROM, flash memory, nonvolatile memory
4. Ultraviolet light (UV) erasable programmable ROM

9.8 Field-Programmable Gate Arrays

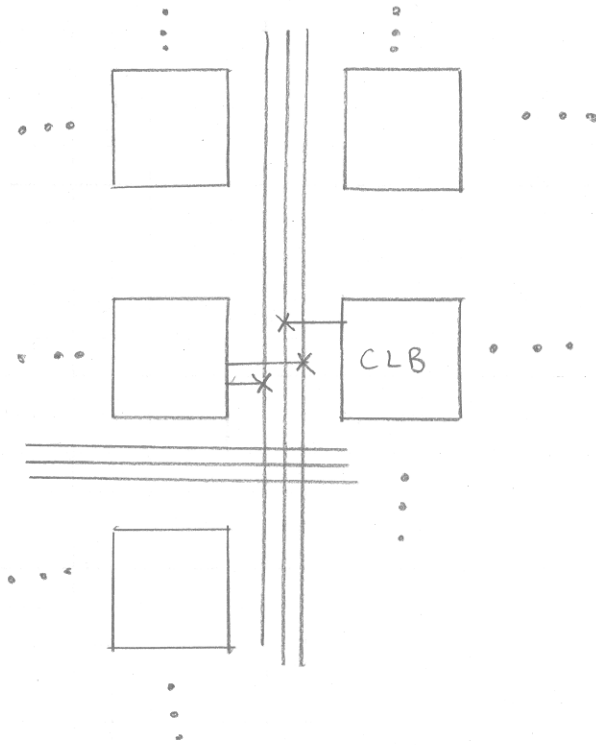
Making custom integrated circuits is expensive and time consuming:

Cost to design and pay for masks (similar to a photographic negative) for each layer of an I.C. can be \$1000 \rightarrow \$25,000 each, usually 10-30 masks.

Gate Array covers a chip with logic gates and you pay to customize a few top layers of metal wiring

Field-Programmable Gate Array (FPGA)

Last layer of connections done with a reconfigurable network circuit (through software).



User programs:

- Small logic blocks, configurable logic blocks (CLBs)
- Connections between blocks

22-141 50 SHEETS
22-142 100 SHEETS
22-144 200 SHEETS

